

| <b>Semester</b> | <b>CORE COURSE<br/>(12)</b> | <b>Ability Enhancement<br/>Compulsory Course<br/>(AECC)<br/>(2)</b> | <b>Skill Enhancement<br/>Course (SEC) (2)</b> | <b>Discipline<br/>Specific<br/>Elective DSE<br/>(4)</b> |
|-----------------|-----------------------------|---|---|---|
| I               | Differential Calculus       | AECC1   |   |   |
|                 | DSC-2A                      |   |   |   |
|                 | DSC-3A                      |   |   |   |
| II              | Algebra                     | AECC2   |   |   |
|                 | DSC-2B                      |   |   |   |
|                 | DSC-3B                      |   |   |   |
| III             | Real Analysis               |   | SEC1  |   |
|                 | DSC-2C                      |   |   |   |
|                 | DSC-3C                      |   |   |   |
| IV              | Differential<br>Equations   |   | SEC2  |   |
|                 | DSC-2D                      |   |   |   |
|                 | DSC-3D                      |   |   |   |
| V               |                             |   | SEC3  | DSE-1A  |
|                 |                             |   |   | DSE-2A  |
|                 |                             |   |   | DSE-3A  |
| VI              |                             |   | SEC4  | DSE-1B  |
|                 |                             |   |   | DSE-2B  |
|                 |                             |   |   | DSE-3B  |

**Discipline Specific Electives (DSE)**

**DSE 1A (choose one)**

1. Mechanics

**DSE 1B (choose one)**

1. Complex Analysis

**Skill Enhancement Course (SEC)**

**SEC 1 (choose one)**

1. Analytical Geometry

**SEC 2 (choose one)**

1. Vector Calculus

**SEC 3 (choose one)**

1. Probability and Statistics

**SEC 4 (choose one)**

1. Boolean Algebra

## Details of Courses under B.Sc. Mathematical Sciences

| Course   | *Credits           |                    |
|--|--------------------|--------------------|
|  | Theory + Practical | Theory + Tutorials |
| <b>I. Core Course</b><br>(12 Papers)<br>04 Courses from each of the<br>03 disciplines of choice  | $12 \times 4 = 48$ | $12 \times 5 = 60$ |
| <b>Core Course Practical / Tutorial*</b><br><b>(12 Practical/ Tutorials*)</b><br>04 Courses from each of the<br>03 Disciplines of choice                                       | $12 \times 2 = 24$ | $12 \times 1 = 12$ |
| <b>II. Elective Course</b><br><b>(6 Papers)</b><br>Two papers from each discipline of choice<br>including paper of interdisciplinary nature.                                   | $6 \times 4 = 24$  | $6 \times 5 = 30$  |
| <b>Elective Course Practical / Tutorials*</b><br><b>(6 Practical / Tutorials*)</b><br>Two Papers from each discipline of choice<br>including paper of interdisciplinary nature | $6 \times 2 = 12$  | $6 \times 1 = 6$   |
| <b>• Optional Dissertation or project work in place of one Discipline elective paper (6 credits) in 6th Semester</b>   |                    |                    |
| <b>III. Ability Enhancement Courses</b>  |                    |                    |
| 1. <b>Ability Enhancement Compulsory</b> $2 \times 2 = 4$<br>(2 Papers of 2 credits each)<br><b>Environmental Science</b><br><b>English/MIL Communication</b>                  |                    | $2 \times 2 = 4$   |

2. **Skill Enhancement Course**       $4 \times 2 = 8$

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**(Skill Based) (4 Papers of 2 credits each)**

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**Total credit = 120**

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**Institute should evolve a system/policy about ECA/ General Interest/ Hobby/ Sports/ NCC/ NSS/ related courses on its own.**

**\*wherever there is practical there will be no tutorials and vice-versa**

## SEMESTER-I

### **DSC -1 (A): Differential Calculus**

Limit and Continuity ( $\epsilon$  and  $\delta$  definition), Types of discontinuities, Differentiability of functions, Successive differentiation, Leibnitz's theorem, Partial differentiation, Euler's theorem on homogeneous functions.

Tangents and normals, Curvature, Asymptotes, Singular points, Tracing of curves. Parametric representation of curves and tracing of parametric curves, Polar coordinates and tracing of curves in polar coordinates.

Rolle's theorem, Mean Value Theorems, Taylor's Theorem with Lagrange's & Cauchy's forms of remainder. Taylor's series, Maclaurin's series of  $\sin x$ ,  $\cos x$ ,  $e^x$ ,  $\log(1+x)$ ,  $(1+x)^m$ , Applications of Mean Value theorems to Monotonic functions and inequalities. Maxima & Minima. Indeterminate forms.

### **Books Recommended**

1. H. Anton, I. Birens and S. Davis, *Calculus*, John Wiley and Sons, Inc., 2002.
2. G.B. Thomas and R.L. Finney, *Calculus*, Pearson Education, 2007.

## SEMESTER-II

### **DSC-1(B): Algebra**

Definition and examples of groups, examples of abelian and non-abelian groups, the group  $Z_n$  of integers under addition modulo  $n$  and the group  $U(n)$  of units under multiplication modulo  $n$ . Cyclic groups from number systems, complex roots of unity, circle group, the general linear group  $GL_n(n, \mathbb{R})$ , groups of symmetries of (i) an isosceles triangle, (ii) an equilateral triangle, (iii) a rectangle, and (iv) a square, the permutation group  $Sym(n)$ , Group of quaternions.

Subgroups, cyclic subgroups, the concept of a subgroup generated by a subset and the commutator subgroup of group, examples of subgroups including the center of a group. Cosets, Index of subgroup, Lagrange's theorem, order of an element, Normal subgroups: their definition, examples, and characterizations, Quotient groups.

Definition and examples of rings, examples of commutative and non-commutative rings: rings from number systems,  $Z_n$  the ring of integers modulo  $n$ , ring of real quaternions, rings of matrices, polynomial rings, and rings of continuous functions. Subrings and ideals, Integral domains and fields, examples of fields:  $Z_p$ ,  $Q$ ,  $R$ , and  $C$ . Field of rational functions.

### **Books Recommended**

1. John B. Fraleigh, *A First Course in Abstract Algebra*, 7th Ed., Pearson, 2002.
2. M. Artin, *Abstract Algebra*, 2nd Ed., Pearson, 2011.
3. Joseph A Gallian, *Contemporary Abstract Algebra*, 4th Ed., Narosa, 1999.
4. George E Andrews, *Number Theory*, Hindustan Publishing Corporation, 1984.

## SEMESTER III

### **DSC-1(C): Real Analysis**

Finite and infinite sets, examples of countable and uncountable sets. Real line, bounded sets, suprema and infima, completeness property of  $\mathbb{R}$ , Archimedean property of  $\mathbb{R}$ , intervals. Concept of cluster points and statement of Bolzano-Weierstrass theorem.

Real Sequence, Bounded sequence, Cauchy convergence criterion for sequences. Cauchy's theorem on limits, order preservation and squeeze theorem, monotone sequences and their convergence (monotone convergence theorem without proof).

Infinite series. Cauchy convergence criterion for series, positive term series, geometric series, comparison test, convergence of p-series, Root test, Ratio test, alternating series, Leibnitz's test (Tests of Convergence without proof). Definition and examples of absolute and conditional convergence.

Sequences and series of functions, Point wise and uniform convergence.  $M_n$ -test, M-test, Statements of the results about uniform convergence and integrability and differentiability of functions, Power series and radius of convergence.

#### **Books Recommended**

1. T. M. Apostol, *Calculus* (Vol. I), John Wiley and Sons (Asia) P. Ltd., 2002.
2. R.G. Bartle and D. R Sherbert, *Introduction to Real Analysis*, John Wiley and Sons (Asia) P. Ltd., 2000.
3. E. Fischer, *Intermediate Real Analysis*, Springer Verlag, 1983.
4. K.A. Ross, *Elementary Analysis- The Theory of Calculus Series-* Undergraduate Texts in Mathematics, Springer Verlag, 2003.

### **SEC -1: Analytical Geometry**

Techniques for sketching parabola, ellipse and hyperbola. Reflection properties of parabola, ellipse and hyperbola. Classification of quadratic equations representing lines, parabola, ellipse and hyperbola. Spheres, Cylindrical surfaces. Illustrations of graphing standard quadric surfaces like cone, ellipsoid.

#### **Books Recommended**

1. G.B. Thomas and R.L. Finney, *Calculus*, 9th Ed., Pearson Education, Delhi, 2005.
2. H. Anton, I. Bivens and S. Davis, *Calculus*, John Wiley and Sons (Asia) Pvt. Ltd., 2002.
3. S.L. Loney, *The Elements of Coordinate Geometry*, McMillan and Company, London.
4. R.J.T. Bill, *Elementary Treatise on Coordinate Geometry of Three Dimensions*, McMillan India Ltd., 1994.

## SEMESTER-IV

### **DSC-1(D): Differential Equations**

First order exact differential equations. Integrating factors, rules to find an integrating factor. First order higher degree equations solvable for  $x$ ,  $y$ ,  $p$ . Methods for solving higher-order differential equations. Basic theory of linear differential equations, Wronskian, and its properties. Solving a differential equation by reducing its order.

Linear homogenous equations with constant coefficients, Linear non-homogenous equations, The method of variation of parameters, The Cauchy-Euler equation, Simultaneous differential equations, Total differential equations.

Order and degree of partial differential equations, Concept of linear and non-linear partial differential equations, Formation of first order partial differential equations, Linear partial differential equation of first order, Lagrange's method, Charpit's method. Classification of second order partial differential equations into elliptic, parabolic and hyperbolic through illustrations only.

#### **Books Recommended**

1. Shepley L. Ross, *Differential Equations*, 3rd Ed., John Wiley and Sons, 1984.
2. I. Sneddon, *Elements of Partial Differential Equations*, McGraw-Hill, International Edition, 1967.

### **SEC -3: Vector Calculus**

Differentiation and partial differentiation of a vector function. Derivative of sum, dot product and cross product of two vectors.

Gradient, divergence and curl.

#### **Books Recommended**

1. G.B. Thomas and R.L. Finney, *Calculus*, 9th Ed., Pearson Education, Delhi, 2005.
2. H. Anton, I. Bivens and S. Davis, *Calculus*, John Wiley and Sons (Asia) P. Ltd. 2002.
3. P.C. Matthew's, *Vector Calculus*, Springer Verlag London Limited, 1998.



## SEMESTER-V

### **DSE -1(A): Mechanics**

Conditions of equilibrium of a particle and of coplanar forces acting on a rigid Body, Laws of friction, Problems of equilibrium under forces including friction, Centre of gravity, Work and potential energy. Velocity and acceleration of a particle along a curve: radial and transverse components (plane curve), tangential and normal components (space curve), Newton's Laws of motion, Simple harmonic motion, Simple Pendulum, Projectile Motion.

#### **Books Recommended**

1. A.S. Ramsay, *Statics*, CBS Publishers and Distributors (Indian Reprint), 1998.
2. A.P. Roberts, *Statics and Dynamics with Background in Mathematics*, Cambridge University Press, 2003.

### **SEC -3: Probability and Statistics**

Sample space, probability axioms, real random variables (discrete and continuous), cumulative distribution function, probability mass/density functions, mathematical expectation, moments, moment generating function, characteristic function, discrete distributions: uniform, binomial, Poisson, continuous distributions: uniform, normal, exponential.

Joint cumulative distribution function and its properties, joint probability density functions, marginal and conditional distributions, expectation of function of two random variables, conditional expectations, independent random variables.

#### **Books Recommended:**

1. Robert V. Hogg, Joseph W. McKean and Allen T. Craig, *Introduction to Mathematical Statistics*, Pearson Education, Asia, 2007.
2. Irwin Miller and Marylees Miller, John E. Freund, *Mathematical Statistics with Application*, 7th Ed., Pearson Education, Asia, 2006.
3. Sheldon Ross, *Introduction to Probability Model*, 9th Ed., Academic Press, Indian Reprint, 2007.

## SEMESTER -VI

### **DSE -1(B): Complex Analysis**

Limits, Limits involving the point at infinity, continuity. Properties of complex numbers, regions in the complex plane, functions of complex variable, mappings. Derivatives, differentiation formulas, Cauchy-Riemann equations, sufficient conditions for differentiability.

Analytic functions, examples of analytic functions, exponential function, Logarithmic function, trigonometric function, derivatives of functions, definite integrals of functions. Contours, Contour integrals and its examples, upper bounds for moduli of contour integrals. Cauchy-Goursat theorem, Cauchy integral formula.

Liouville's theorem and the fundamental theorem of algebra. Convergence of sequences and series, Taylor series and its examples.

Laurent series and its examples, absolute and uniform convergence of power series.

#### **Books Recommended**

1. James Ward Brown and Ruel V. Churchill, *Complex Variables and Applications*, 8th Ed., McGraw – Hill International Edition, 2009.
2. Joseph Bak and Donald J. Newman, *Complex analysis*, 2nd Ed., Undergraduate Texts in Mathematics, Springer-Verlag New York, Inc., New York, 1997.

### **SEC -4: Boolean Algebra**

Definition, examples and basic properties of ordered sets, maps between ordered sets, duality principle, maximal and minimal elements, lattices as ordered sets, complete lattices, lattices as algebraic structures, sublattices, products and homomorphisms.

Definition, examples and properties of modular and distributive lattices, Boolean algebras, Boolean polynomials, minimal forms of Boolean polynomials, Quinn-McCluskey method, Karnaugh diagrams, switching circuits and applications of switching circuits.

#### **Books Recommended:**

1. B A. Davey and H. A. Priestley, *Introduction to Lattices and Order*, Cambridge University Press, Cambridge, 1990.
2. Rudolf Lidl and Günter Pilz, *Applied Abstract Algebra*, 2nd Ed., Undergraduate Texts in Mathematics, Springer (SIE), Indian reprint, 2004.